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袁春宇　曹阳　邓勇　张书练

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Improving the measurement accuracy of refractive index of GaAs and Sapphire Crystal by laser feedback interferometry

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Abstract: GaAs and Sapphire Crystal has been widely used in infrared region, optoelectronics field and military equipment, so the measurement of refractive index of two materials is of great significance to optical design, metrological inspection and industrial application. To improve the measurement accuracy of refractive index of two materials, microchip laser feedback interferometer technology was used to simultaneously measure refractive index and thickness. The system combined heterodyne modulation and quasi-common path to compensate for airflow and vibration, so it has the characteristics of high sensitivity, high precision and high stability, especially the simultaneous measurement and only the material needs to be processed into flake rather than prism shape. The experimental results demonstrate that the measurement accuracy of refractive index of GaAs and Sapphire Crystal (under ordinary light) has been enhanced to 10^{-3} and 10^{-4} respectively and thickness is 10^{-4} mm.

Key words: GaAs; Sapphire Crystal; feedback interferometry; refractive index; accuracy

以激光回馈干涉技术提高砷化镓和
蓝宝石晶体的折射率测量精度

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摘　要： 砷化镓和蓝宝石晶体已经广泛应用于红外领域、光电领域和军事设备，因此两种材料的折射率测量对光学设计、计量检测和工业应用具有重要意义。为提高两种材料折射率的测量精度，采用微片激光回馈干涉技术同时测量折射率和厚度。此系统结合外差调制和准公共路径对空气气流和振动进行补偿，因此具有高灵敏度、高精度和高稳定性的特点，特别是同时测量性以及仅需将样品加工成薄片状而非棱柱形。实验结果表明，砷化镓和蓝宝石晶体(在寻常光下)的折射率测量精度提高到 10^{-3} 和 10^{-4}，且厚度的精度均为 10^{-4} mm。

关键词： 砷化镓； 蓝宝石； 回馈干涉； 折射率； 精度

0　Introduction

With the development of science and technology, optical crystals and semiconductors are widely used in optical system design, gem identification, medicine, chemical engineering and other fields, especially the typical optical crystal Sapphire Crystal and the typical semiconductor material GaAs. The Sapphire Crystal is usually used in intelligent instruments, laser window materials, infrared military equipment and other regions. The use of Sapphire Crystal in military photovoltaic equipment is very wide. For example, when it used as a window material of a military photovoltaic device, it is necessary to accurately calculate the refractive index and transmittance to effectively transmit radiation of ultraviolet to medium infrared bands. GaAs is used in infrared light emitting diode, lasers and many other optoelectronics. GaAs is usually used as the material of solar cells, and the refractive index is a key parameter to the film layer design to affect the photoelectric conversion rate. High-precision measurement of refractive index of Sapphire Crystal and GaAs is meaningful for optical design and metrological inspection. The gem refractometer is commonly used in the gem identification field to measure the refractive index of Sapphire Crystal, and its accuracy is 10^{-3}[1]. The book (*Optical Handbook*[2]) for the refractive index accuracy of GaAs is 10^{-2}. Therefore, further research is needed to improve measurement precision of refractive index. Currently, the most accurate method for measuring refractive index is the minimum deviation angle method (10^{-6})[3–5], but it requires prismatic sample material, high sample requirements and high cost. In addition, the measurement equipment is huge and has strict environmental conditions, so it cannot be universally applied. Abbé refractometer widely used in industrial and laboratory and precision is 10^{-4}, but the measurement range is between 1.3-1.7. The ellipsometry can be measured refractive index in a wide wavelength, but the accuracy is 10^{-2}. The m-lines method is used to measure refractive index of the film by a prism coupler[6], providing an accuracy of 10^{-3}. In contrast, interferometry has the advantages of simple sample material processing, wide measurement range, low cost and high precision. At present, the commonly used methods include Michelson interferometer[7–8], Fabry-Perot interferometer[9–10], Mach-Zehnder interferometer[11–12], and self-mixing interferometer [13], etc. These methods are dependent on laser intensity fringes by the sample material optical path change. If the contrast of interference fringes is reduced, the measurement resolution will be lower. Further, the whole measurement optical path is the dead path, so there are environmental interference including air flow and vibration for these interferometers, making measurement accuracy and repeatability easily affected by environment and laser power fluctuations.

In order to improve the accuracy of GaAs and Sapphire Crystal, the article decides to avoid environmental disturbances and overcome interference contrast problems, so the paper proposes the microchip laser feedback interferometry (MLFI) at 1 064 nm to measure refractive index and thickness. In this paper, MLFI combines the quasi-common path structure and the frequency shifted optical feedback to realize the compensation of dead-distance error and the heterodyne modulation of laser intensity, so the impact of environmental interference is eliminated and the measurement accuracy is improved. Compared with traditional methods, the measurement method can simultaneously measure refractive index and thickness and only the material needs to be processed into flake rather than prism shape. The measurement accuracy of refractive index of GaAs and Sapphire Crystal (under ordinary light) has been improved. The precision of refractive index of GaAs and Sapphire Crystal are better than 10^{-3} and 10^{-4} respectively and thickness is 10^{-4} mm. Therefore, it is very suitable and meaningful to use MLFI to simultaneously measure refractive index and thickness for improving the measurement accuracy of GaAs and Sapphire Crystal.

1 Experiment system

The schematic diagram of experimental system is shown in Fig. 1. ML is a microchip Nd:YVO$_4$ laser light source pumped by two same LDs and ML outputs two parallel laser beams. Both laser beams are fundamental transverse modes and linearly polarized single longitudinal modes. The working wavelength of these two lasers is both 1 064 nm. The measurement mirror M$_E$ is a light wedge covered with copper foil, and its front surface is the reflective surface. Acousto-optic modulators (AOM$_1$ and AOM$_2$ are YSGMN from SIPAT) are placed in the optical feedback path to realize the frequency shifting. The reference mirror M$_R$ is also a light wedge covered with copper foil. It is placed between the two acousto-optic modulators and M$_E$ to eliminate feedback environmental interference. L$_1$ and L$_2$ are two lenses used to focus the light beams (B$_1$ and B$_2$) on M$_R$ and M$_E$ respectively. The light beams (B$_1$ and B$_2$) are reference and measurement light. S is the solid material sample which is polished thin wafer. S is located between M$_R$ and
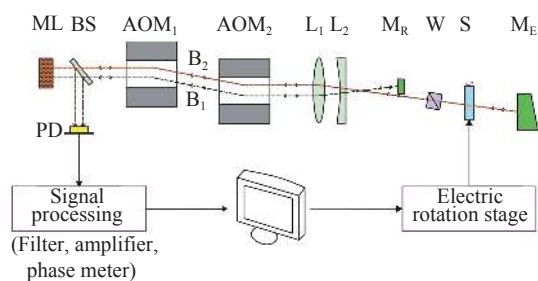

Fig.1 System for measuring based on laser feedback interferometry. ML: Nd:YVO$_4$ microchip laser; BS: Beam splitter; PD: Photodetector; AOM$_1$ and AOM$_2$: Acousto-optic modulators; L$_1$ and L$_2$: Lens; W: Wollaston prism. M$_R$: Reference mirror; S: Material; M$_E$: Measurement mirror

M$_E$, and it is controlled to rotate by an electric controlled rotation stage (MRS211 from Beijing Beiguang Century Instrument Co., Ltd.). The photodetector PD contains two PIN photodiodes.

Two beams of light emitted by the light source ML pass through AOM$_1$ and AOM$_2$ and are divided into eight beams. The optical path for differential frequency shift of two acousto-optic modulators is shown in Fig. 2. The output laser beam ② and ⑥ which underwent -1-order diffraction and +1-order diffraction are respectively used as reference light and measurement light, and the frequency shift amount is Ω ($\Omega_2-\Omega_1$). M$_R$ and M$_E$ can be adjusted so that the feedback light can return to the laser cavity passing through AOM$_1$ and AOM$_2$, so the total frequency shift amount of B$_1$ and B$_2$ are both 2Ω. Among them, the measurement light B$_2$ through the Wollaston prism W is divided into two beams (ordinary ray and extraordinary ray), and it can be chosen which beam as the measurement light according to the anisotropy of materials. The two feedback optical signals B$_1$ and B$_2$ after heterodyne modulation are respectively received by the two PIN photodiodes and converted into electrical signals. According to the rate equation model, the power modulation of the frequency shift laser feedback after the light returning to the laser is given by[14]

$$\Delta I(2\Omega) = \kappa G(2\Omega)\cos\left[2\pi(2\Omega)t - \varphi + \varphi_s\right] \qquad (1)$$

where ΔI is the intensity of laser B$_1$ and B$_2$ respectively, κ is feedback light strength factor, G is the gain amplification factor, which is related to the value of frequency shifting, ϕ is the external cavity phase (ϕ_m or ϕ_r), and ϕ_s is fixed phase. For the material with large internal absorption and low transmittance, the system is based on the high sensitivity characteristics of frequency
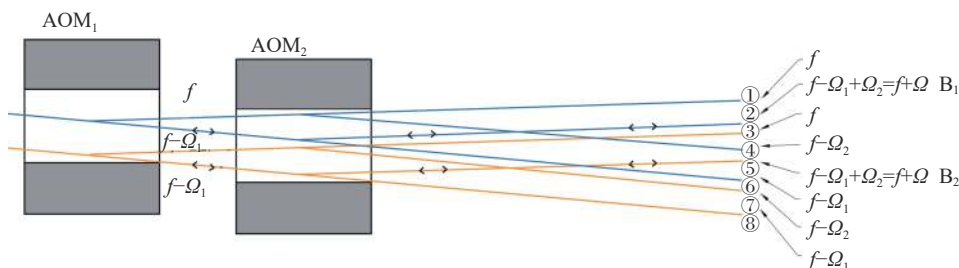

Fig.2 Schematic diagram of optical path for differential frequency shift of acousto-optic modulators. ①~⑧: Eight output laser beams

shifting light feedback, so the reduction of the interference fringe contrast will not cause the measurement resolution to decrease.

According to the equation, the wave of intensity modulation curve is cosine, and the modulation frequency is the frequency shift of feedback light (2Ω). As the material is rotated by an electric controlled rotation stage, the phase changed by the optical path change. $\Delta\phi_r$ is reference signal between ML and M_R, and $\Delta\phi_m$ is measurement signal between ML and M_E. $\Delta\phi_m - \Delta\phi_r$ is compensation for impact of environmental disturbances. In the experiment, the driving frequency of AOM_1 and AOM_2 are 70 MHz and 70.4 MHz respectively, the power modulation frequency (2Ω) of the reference light and the measurement light are both 800 kHz. The transparent surface is coated by the antireflecting film to prevent the laser from being reflected by the edge surface of the acousto-optic medium to form feedback.

2 Experiments and results

When electric rotation stage is controlled to rotate, the optical path changes in the material with rotating. As shown in Figure 3, when the angle between the normal line of the material surface and the light is θ, the optical distance L in the material is

$$L = \frac{nd}{\cos i} + n_0 x - \frac{n_0 d}{\cos i}\cos(q - i) \qquad (2)$$

where d is the thickness of material, n denotes the refractive index to be measured, i denotes the refraction angle in the material, n_0 denotes the air refractive index, and x is geometric length from optical position incident on the material to the measurement mirror. According to Snell equation [15]
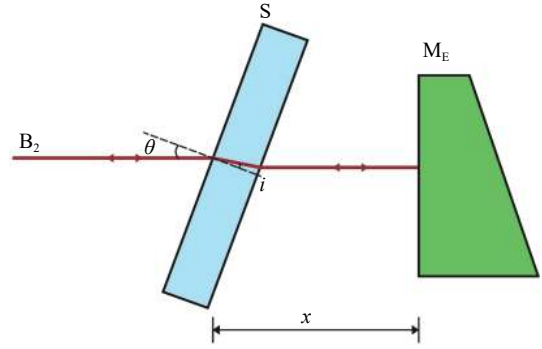

Fig.3 Schematic diagram of the sample material optical path

$$n_0\sin\theta = n\sin i \qquad (3)$$

derive as

$$L = n_0 x - n_0 d\cos\theta + d\sqrt{n^2 - n_0^2\sin^2\theta} \qquad (4)$$

Assuming that the angle between the surface normal of material and the beam before rotation is θ_0, and the angle after rotation is θ, the optical path change ΔL is

$$\Delta L = \frac{\lambda}{2\pi n_0}(\Delta\phi_m - \Delta\phi_r) = \left[\sqrt{n^2 - n_0^2\sin^2\theta} - n_0\cos\theta - \sqrt{n^2 - n_0^2\sin^2\theta_0} + n_0\cos\theta_0 \right] \qquad (5)$$

where the optical path change $\Delta\phi_r$ of reference signal comes from the air disturbance between ML and M_R and the thermal effect of the acousto-optic modulators, and the optical path change $\Delta\phi_m$ of the measurement signal comes from the air disturbance between ML and M_E, thermal effect and the optical path change. When the material is rotated, θ and ΔL selected at multiple angles are substituted into equation (5) to solve this over-determined equation expressed by equation (6). It excludes the effect of thickness measurement uncertainty on refractive index accuracy.

$$\left. \begin{aligned}
\Delta L_1 &= d\left[\sqrt{n^2 - n_0^2\sin^2\theta_1} - n_0\cos\theta_1 - \sqrt{n^2 - n_0^2\sin^2\theta_0} + n_0\cos\theta_0 \right] \\
\Delta L_2 &= d\left[\sqrt{n^2 - n_0^2\sin^2\theta_2} - n_0\cos\theta_2 - \sqrt{n^2 - n_0^2\sin^2\theta_0} + n_0\cos\theta_0 \right] \\
\Delta L_3 &= d\left[\sqrt{n^2 - n_0^2\sin^2\theta_3} - n_0\cos\theta_3 - \sqrt{n^2 - n_0^2\sin^2\theta_0} + n_0\cos\theta_0 \right] \\
&\vdots \\
\Delta L_x &= d\left[\sqrt{n^2 - n_0^2\sin^2\theta_x} - n_0\cos\theta_x - \sqrt{n^2 - n_0^2\sin^2\theta_0} + n_0\cos\theta_0 \right]
\end{aligned} \right\} \Rightarrow n,d \qquad (6)$$

In the experiment, the material S is polished thin wafer which is Sapphire Crystal or GaAs. Because sapphire is an anisotropic uniaxial crystal, it has two refractive indices. Choose ordinary ray of W as the measurement light B_2. The thickness of Sapphire Crystal and GaAs are 0.302 mm and 0.686 mm respectively measured by a micrometer. The air sensor is used to detect the air in the experiment. The indoor temperature of Sapphire Crystal is 23.34 ℃, the air pressure is 101.93 kPa, the relative humidity is 18.5%, and the air refractive index n_0 is calculated as 1.0002678 by the modified Edlén equation[16]. For GaAs, they are 23.60 ℃, 101.89 kPa, 16.5%, and 1.0002675. Considering the transmittance of the materials and reducing the measurement uncertainty requirement, decide that Sapphire Crystal is rotated from 0° to 30° with pausing every two degrees, and GaAs from 0° to 20° with pausing every angle. The optical path difference of rotating material at each angle is measured 20 times within 20 seconds. The average optical path difference is shown in Table 1 and Table 2.

Substitute the experiment data in Table 1 and Table 2 and n_0 into equation (5) by fitting refractive index and thickness. The theoretical curve and experimental data points are drawn in Fig. 4(a). It is shown that, consistent with the experimental data, the solution of the Sapphire Crystal n is 1.7551, d is 0.3017 mm, the GaAs n is 3.4653, and d is 0.6862 mm. The difference between theoretical

Tab.1 The average optical path difference in Sapphire Crystal with angle

Rotation angle/(°)	Optical path change/nm	Rotation angle/(°)	Optical path change/nm
1	145	11	8924
2	354	12	10693
3	689	13	12594
4	1186	14	14502
5	1827	15	16679
6	2598	16	19042
7	3558	17	21524
8	4674	18	24134
9	6015	19	26870
10	7482	20	30037

Tab.2 The average optical path difference in GaAs with angle

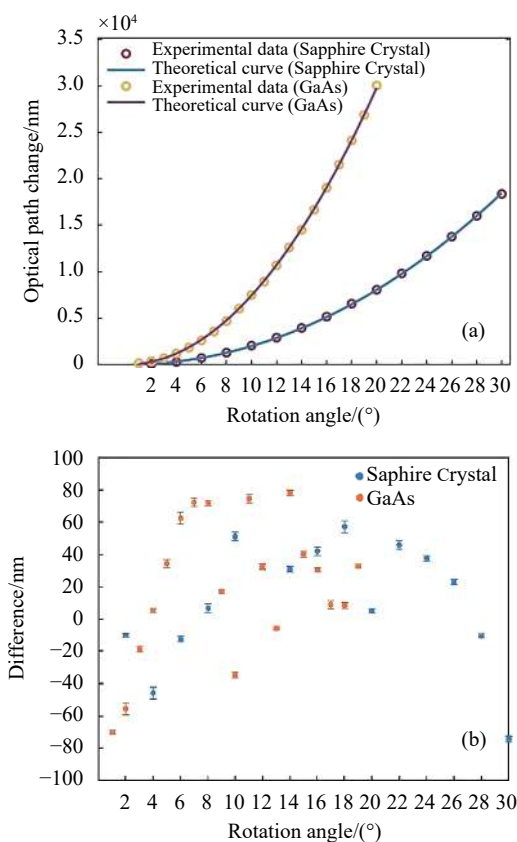| Rotation angle/(°)	Optical path change/nm	Rotation angle/(°)	Optical path change/nm
2	69	18	6550
4	270	20	8047
6	700	22	9811
8	1275	24	11703
10	2036	26	13771
12	2896	28	16006
14	3937	30	18365
16	5158		

Fig.4 (a) Theoretical and experimental data of optical path change of two materials with angle of rotation; (b) Difference between theoretical fit data and experimental data

fit data and experimental data of optical path change at every angle is presented in Fig. 4(b), and the difference range is from −80-80 nm.

There are five times of the measurement of Sapphire Crystal and GaAs, and the measurement results are presented in Table 3. Calculate the measurement average

value (refractive index and thickness) and type A evaluation of uncertainty[17](that is, the standard deviation calculated by the Bessel equation[18]). From Table 3, the refractive index of Sapphire Crystal is 1.7550 ± 0.0005. The reference value is based on the value calculated by Sellmeier equation[2], which is 1.7545, so the deviation of the experimental data with the reference data is 0.0005. The measurement accuracy of Sapphire Crystal reaches 10^{-4} and the material does not need to be processed into prismatic shape. However, the accuracy of ellipsometry method and m-lines method are 10^{-2} and 10^{-3} respectively, and the common reflective gem refracto-meter is 10^{-3}. The refractive index of GaAs is 3.4719 ± 0.0039. The reference refractive index value is 3.4727 which is calculated by Sellmeier equation[19], so the deviation of the experimental data with the reference data is 0.0008. The measurement accuracy range of GaAs is between 10^{-3}-10^{-4}. However, the ellipsometry method accuracy is 10^{-2} and GaAs is beyond the measurement range of Abbé refractometer. From Table 3, the thickness of Sapphire Crystal is (0.3022 ± 0.0004) mm, and the thickness measured by micrometer is (0.302 ± 0.001) mm. The thickness of GaAs is (0.6861 ± 0.0001) mm, and the thickness measured by micrometer is (0.686 ± 0.001) mm. Therefore, the results are satisfactory and the accuracy has been improved.

There are several reasons for refractive index measurement error Δn. First of all, the material composition, processing technology and surface morphology are the main reasons for the measurement error Δn. Among them, the main component of Sapphire Crystal is Al_2O_3, which contains the trace elements

Tab.3 Measurement results

Number	Sapphire Crystal		GaAs	
	n	d/mm	n	d/mm
1	1.7553	0.3028	3.4653	0.6862
2	1.7551	0.3026	3.4759	0.6861
3	1.7539	0.3019	3.4739	0.6860
4	1.7554	0.3018	3.4696	0.6859
5	1.7551	0.3017	3.4749	0.6861

titanium (Ti^{4+}) or iron (Fe^{2+}), and different doping concentrations lead to different refraction effects. Due to the different crystal growth process, the melting temperature, the number of pulling times and other steps are also different. However, the temperature, pulling number and other steps will affect refraction results. Secondly, both materials are polished wafers, so the parallelism, roughness and uniformity of their surfaces will affect the measurement accuracy and the corresponding Δn cannot be accurately calculated. In addition, the air refractive index and the laser wavelength will vary with the ambient temperature. In a normal laboratory environment, the refractive index of air changes less than 10^{-5}, and Δn is less than 7×10^{-6}. The frequency-stabilized microchip laser has the wavelength drift $\Delta\lambda$ less than 2.6×10^{-4} nm, and Δn is only 1.94×10^{-7}. Finally, GaAs is a semiconductor material, and refractive index of semiconductor material is complex number because its conductivity is not zero. This article is measuring the real part of the complex refractive index. However, when light is incident on the GaAs sheet obliquely at a certain angle, the extinction coefficient of the semiconductor material (that is, the imaginary part of the complex refractive index) will affect the real part, thereby affecting the measurement data of refractive index.

3 Summary

In conclusion, in order to improve the measurement accuracy of refractive index of GaAs and Sapphire Crystal, the paper use LD-pumped microchip $Nd:YVO_4$ laser feedback interferometry at 1064 nm to simul-taneously measure refractive index and thickness. The experimental results are satisfactory. The experimental measurement uncertainty of refractive index of two materials less than (or equal to) 0.0005 and 0.0039 respectively and the deviation from reference value is lower than 0.0008. The thickness measurement uncertainty is less than 0.0004 mm. The precision of refractive index of GaAs and Sapphire Crystal are 10^{-3}

and 10^{-4} respectively and thickness is 10^{-4}, so the measurement accuracy has been improved. The measurement method is high sensitivity, high precision and high stability. In particular, the measurement is simultaneous and only the material needs to be processed into flake rather than prism shape. Therefore, it is very suitable and meaningful to use the measurement system to measure for improving the accuracy of refractive index measurement. The Sapphire Crystal is usually used in intelligent instruments, laser window materials, infrared military equipment and other regions. GaAs is used in infrared light emitting diode, lasers and many other optoelectronics. High-precision measurement of refractive index and thickness of Sapphire Crystal and GaAs is of great significance to infrared region, optical design and metrological inspection. In the future, it is our duty to optimize this system to other wavelengths and other materials. Moreover, further improving refractive index measurement accuracy of Sapphire Crystal and GaAs is necessary.

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